

# Low Phase Noise & Fast Startup Crystal Oscillator

by

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A thesis submitted in partial fulfillment for the  
degree of Master of Technology

under supervision of

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June 2019



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# Certificate

This is to certify that the thesis titled "**Low Phase Noise & Fast Startup Crystal Oscillator.**" submitted by **Avinash Pandit** (Roll Number - MT17084) for the partial fulfillment for the degree of **Master of Technology in VLSI & Embedded Systems** of the requirements is an original work carried out by him under my supervision. In my opinion, thesis has reached the standards fulfilling the requirements of the regulations relating to the degree. The results contained in the thesis have not been submitted in part or full to any other university or institute for the award of any degree/diploma.

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# *Abstract*

The crystal oscillator is widely used in the electronics industry since it has become one of the essential parts of the reference clock for the Phase-locked loop(PLL). High-performance systems benefit from higher frequency reference clocks. However, there is a real frequency limitation to quartz resonators. Quartz operates up to 1GHz and is not manufactured with today's technology. PLL has more intrinsic noise and has more power consumption. To reduce the overall noise of PLL, the reference clock must have minimum noise. Hence, this works presents the design and implementation of a low phase noise & fast startup crystal oscillator. Generally, crystal oscillators have limited current support depending on their drive level capability. The transconductance gm stage has been proposed by limiting the current which leads to improvement in phase noise. Jitter has been controlled by using the low pass filter. This circuit is capable of ensuring fast startup time with the help of its proposed crystal architecture design and transconductance design, which is presented in this work.

The proposed circuit design is implemented in TSMC 28nm CMOS technology. Two types of power supply have been used as an external and main power supply. The simulation results show the startup time of crystal oscillator from 120us to 150us. The crystal oscillator's current consumption from 362uA to 1.58mA. The phase noise of the crystal oscillator -138dBc/Hz @1KHz. The jitter of the crystal oscillator from 1ps to 3ps. Duty Cycle of the crystal oscillator at different PVT corners is from 46% to 52%.

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*Dedicated to my beloved parents...*

# Chapter 1

## Introduction

Nowadays, a precise and accurate clock is an essential part of the integrated circuits. There are many types of oscillators, which produces a clock for transceivers and digital circuits. In these oscillators, a Crystal oscillator is one of the most stable and accurate clock generator and as a reference clock generator crystal is the most reliable choice [1]. Clock generators such as ring oscillator, LC oscillator, and relaxation oscillator have frequency variation due to changes in supply, process, and temperature. For instance, real-time frequency variation specification of a Bluetooth should be less than the  $\pm 75$  at a 2.4GHz carrier frequency[2]. Total variation in frequency after including, the clock distributor circuits, phase locked loop(PLL) and the reference clock shown in Fig.1.1 must be less than  $\pm 31$  ppm[2]. This specification is difficult to achieve for an on-chip oscillators because temperature variations also caused frequency variations and it is more than  $\pm 1\%$  which is 1000ppm[2]. High quality factor of quartz crystal leads to less frequency variation in crystal, which is better than the CMOS oscillators. Phase noise is dependent on frequency variation. Minimum frequency deviation leads to less phase noise.

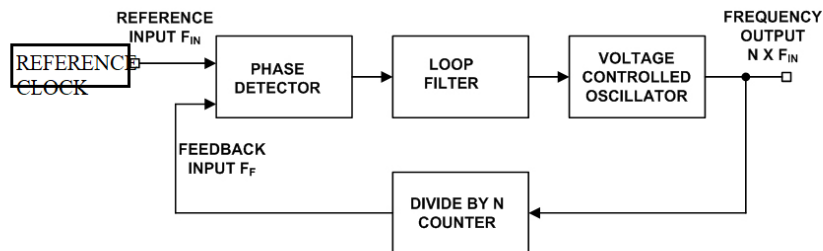


FIGURE 1.1: Block diagram of PLL

Other than frequency variation, one of the crucial aspects is power. When oscillations start, the oscillator requires more current. Which leads to high power consumption. To reduce power in these circuits, there are two modes active and standby mode. The active mode in which power consumption is high, all the circuits are 'ON'. Standby mode in which power consumption is less, required circuits are 'ON'.

It is essential to keep track of the drive power rating of the crystal [3]. Due, to limited power dissipation by a series resistor of the crystal. Excess current at this resistor may lead to destroying the crystal. Hence, current in the crystal must be less than the drive level. Oscillation allowance of the crystal is one of the critical parameter, which depends on amplifier resistance. To have the oscillation in crystal negative resistance provided by the amplifier must be greater than the crystal resistance.

The crystal oscillator deals with a slow startup, many techniques have been listed such as injecting the noise using ring oscillator, these methods lead to decrease the phase noise of the crystal but it increases the overall area of the circuit[4]. A Novel technique has been proposed while limiting the current in the crystal. This technique improves the startup, phase noise and jitter of the crystal oscillator.

## 1.1 Motivation

Due to the impact of technology node scaling, device noise increases and area limits. Which leads to more deviation in frequency. Due to more frequency deviation, data of the transmitter & receiver can detect the wrong data, which leads to failure in data synchronization. Phase noise & reliability of the crystal oscillator degrade. Due to the presence of high load capacitor loop gain of the crystal oscillator reduce. It degrades the startup time of the crystal oscillator. If load capacitance reduces the frequency of the oscillator increases. While improving the loop gain of the crystal oscillator, current consumption increases. Hence, the design suffers from high losses and high currents. Other challenges are aging, overtone frequency of oscillator and losses due to motional inductance. To overcome these challenges an architecture of the crystal oscillator design has been proposed with a transconductance  $g_m$  gain stage to achieve the goal of low phase noise and fast startup.

## 1.2 Thesis Outline

The main objective of this thesis is to design a low phase noise and fast startup & higher reliability crystal oscillator circuit for on chip clock generation. Several states of

art techniques have been studied and incorporated within the design to address the open design challenges such as oscillation allowance, phase noise, startup, and jitter. TSMC 28nm CMOS technology has been used for the design of crystal oscillator. This thesis primarily introduces the behavior of crystal oscillator and its design challenges.

The specification for inner power supply is from 1.6v to 2.0v & the outer power supply is from 0.8v to 1.0v. The current consumption for the crystal in the range from 300uA to 1.8mA. In low power mode, the current consumption is from 300uA to 1.2mA. Oscillation Swing of the crystal oscillator in the range from 0v to 1.8v. The square wave clock generation from crystal is in the range from 0v to 0.9v. The gm stages must provide the current in the range from 600uA to 1.2mA. The Oscillation allowance must be greater than 5, to produce stable oscillation. Startup time must be lower than 1ms. The OFF chip capacitor value is 10pF. The power drive value of crystal is 200uW.

The phase noise specification for crystal oscillator is -120dBc/Hz @1KHz and -150dBc/Hz @1MHz. Startup time must be lower than 1ms. Jitter must be less than 10ps @(100kHz to 100MHz). However, these specification limits the requirements of  $g_m$  gain stage of the crystal oscillator. The proposed  $g_m$  gain stage has current stability, high gain, large bandwidth, and sufficient area. This proposed work has been verified against different PVT variations.

### 1.3 Structure of the Work

This thesis is divided into 6 chapters to reflect the necessary information that leads up to the complete design of a crystal oscillator.

- **Chapter 2: Crystal Oscillator**

This chapter describes various Crystal Oscillator parameters and its blocks, such as Quality Factor, Resonant Frequency, Overtone, Drive level, Startup Time, Losses. Different types of crystal oscillator design have been described in this section. Oscillation allowance, negative resistance and startup time of crystal has been discussed.

- **Chapter 3: Noise & Jitter Analysis**

This chapter gives an insight into the crystal Oscillator phase noise. It also contains a brief description of the jitter, random noise, and deterministic noise.

- **Chapter 4: Proposed Architecture Design**

This chapter discusses the proposed crystal oscillator design, proposed transconductance  $g_m$  stage design, buffer stage design, and schmitt trigger stage design & its detailed analysis.

- **Results**

This chapter shows the results of the proposed  $g_m$  stage & crystal oscillator design.

- **Conclusions**

This chapter concludes all the findings and contributions of this work and discusses possible future work.

## Chapter 2

# Crystal Oscillator

This chapter provides the main focus on the fundamental property of crystal oscillator. It also discusses the theoretical aspects of the crystal oscillator. The brief discussion on the quartz crystal in section 2.1 & its property for e.g piezoelectric effect, crystal resonance, quality factor, motional impedance, overtone frequency, losses, drive level, aging effects on the crystal. A Later brief discussion on crystal oscillator design, negative resistance, start-up time, oscillation allowance, Feedback Resistor, oscillator transconductance, and load capacitance. LC oscillators are one of the basic oscillators used for tuned circuits. They have poor phase noise and frequency drift due to PVT variations. Crystal oscillator also used in tuned circuits because of its stable oscillations. At resonance, Quartz crystals have high-quality factor(Q) in the range of 10,000 to several thousand. One of the limitations of the crystal oscillator is high Q. In the crystal, loss of energy occurs through the resistance in the quartz material. While energy stored in capacitance and inductor bypassing the current from one component to another component.

### 2.1 Quartz crystal

Quartz crystal has better temperature stability, quality factor, aging effect than other resonators. The advantage of a quartz crystal is more over than a discrete LC oscillator. Quartz crystal has the piezoelectric property that transforms one energy into another (mechanical to electrical or electrical to mechanical). The Piezoelectric effect has its property that it produces mechanical vibrations when the electric field applied to it. The electrical signal produces mechanical vibration. Because this vibration crystal starts to resonate at a certain frequency and amplitude signal becomes larger as the signal goes near to this mechanical vibration.



### 2.1.1 Piezoelectric Effect

As we discussed in the above subsection 2.1, Quartz crystal has a piezoelectric effect and piezoelectric material is used for quartz crystal. Piezoelectric material has a phenomenon. When external stress has been applied to the Crystal, it will be deformed or mechanically strained. The polarity of the electric charge is reversed, due to the strain applied on the crystal. It will revert the direction of charges present on crystal, which changes the polarity. This is called the direct piezoelectric effect, and these properties show by quartz crystals are known as piezoelectric crystals. When an electric field is placed over piezoelectric material, strain started to show over the crystal, because of charges produced by an applied electric field. This will change the crystal dimension. Due to applied reverse electric field effects the reversed strain direction a field. This is known as a converse piezoelectric effect.

### 2.1.2 Equivalent Crystal

TABLE 2.1: Crystal Specification

$R_m$	56.38Ohm
$L_m$	31.714100mH
$C_m$	1.278334fF
$C_0$	0.609577pF

In this subsection, the equivalent circuit of quartz crystal has been shown in Fig.2.1. Specification of the crystal has been shown in Table.2.1. The mechanical behavior of the crystal element is shown by the motional parameters which are  $R_m$ ,  $L_m$ ,  $C_m$ .  $R_m$  is known as motional resistance, mechanical losses represent by  $R_m$ .  $L_m$  is known as motional inductance, it is proportional to the mass of the mechanical resonator.  $C_m$  is known as motional capacitance it is proportional to the inverse of its stiffness. The electrical behavior of crystal shown by  $C_0$ , it also represents shunt capacitance due to the capacitor formed by electrodes. Stable oscillation produced by  $L_m$  and  $C_m$ , which forms a stable resonant circuit, when small  $R_m$  has been used in crystal.

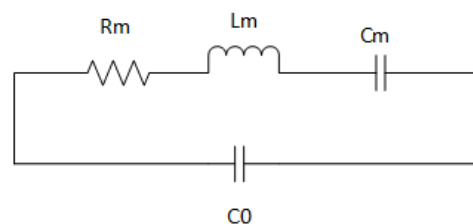


FIGURE 2.1: Quartz Crystal Architecture

### 2.1.3 Quality Factor

The quality or efficiency of the crystal determines by the Quality factor (Q). It is in the range of 10 to 10,000. Typically, crystal has a high Q. High-quality factor leads to narrow bandwidth but frequency stability will be high. Mathematical, Quality factor is defined as:

$$Q = \frac{\text{Energy Stored per cycle}}{\text{Energy Dissipated per cycle}} = \frac{1}{\omega_0 R_m C_m} = \frac{\omega_0 L_m}{R_m} = \frac{1}{R_m} \sqrt{\frac{L_m}{C_m}}$$

### 2.1.4 Crystal Resonant Frequency

In this subsection, the discussion will be on the series frequency and parallel frequency of the crystal. As shown in equ 2.1[5],  $R_m$  is the impedance of the crystal.  $f_0$  is the operating frequency of a crystal and it lies between parallel and series frequency. The range between series and parallel frequency is known as crystal bandwidth. i.e  $f_s < f_0 < f_p$ . The resonant frequency of Crystal at that point, where (XL = XC) which means inductance and capacitance of crystal cancels each other. When crystal operates at  $f_s$ , crystal impedance will be minimum. When crystal operates at  $f_p$ , crystal impedance will be maximum.

$$Z = \frac{j}{\omega} * \frac{\omega^2 * L_m * C_m - 1}{(C_0 + C_m) - \omega^2 * L_m * C_m * C_0} \quad (2.1)$$

A crystal has two resonant frequencies

(i). The series-resonant  $f_s$ [5], is derived from equ 2.1 when impedance  $Z=0$ , it is due to  $C_m$  and  $L_m$ .

$$f_s = \frac{1}{2\pi\sqrt{L_m C_m}}$$

(ii). The parallel-resonant  $f_p$ [5], is derived from equ 2.1 when impedance  $Z=\infty$ , it is due to  $C_0$ ,  $C_m$  and  $L_m$ .

$$f_p = \frac{1}{2\pi\sqrt{L_m \frac{C_m C_0}{C_m + C_0}}} = f_s \sqrt{1 + \frac{C_m}{C_0}}$$

### 2.1.5 Motional Impedance

In this section, we will discuss the motional impedance of crystal, As discussed in above section that due to high quality factor, the bandwidth of the crystal narrows down. Motional impedance changes due to high quality factor. The main dependency of motional impedance shown over the motional current( $i_m$ ). Equ.2.4[6] concludes, negligible current flow through the crystal which will be sinusoidal and it has no voltage dependency. The complex motional impedance is given by[6]:

$$Z_m = R_m + J\omega_0 L_m + \frac{1}{j\omega_0 C_m} \quad (2.2)$$

It can be also written as:

$$Z_m = R_m + \frac{j\omega_0}{C_m} \cdot \frac{\omega_0 + \omega_s}{\omega_s} \cdot \frac{\omega_0 - \omega_s}{\omega_s} = R_m + j \frac{2P}{\omega_0 C_m} \quad (2.3)$$

$$i_m(t) = |i_m| \sin(\omega_0 t) \quad (2.4)$$

### 2.1.6 Overtone

Crystal operates at its fundamental frequency. Crystal banks will get thinner due to increment in its frequency. Then, one option is to use its odd harmonics. Odd harmonics are known as the odd multiple frequencies of the fundamental, 3rd, 5th, 7th, e.t.c. which is close to overtones oscillation of the crystal. crystal may also have many other modes of operation which can be exercised. These modes are unwanted and maybe excited to lesser or greater degrees by different circuits. Overtone frequency is not the exact multiple of the harmonics of the fundamental frequency, but it close to the fundamental frequency. The Only fundamental frequency has been used in this thesis.

### 2.1.7 Aging

In this subsection, we will be going to discuss the aging of the crystal oscillator. Due to change in frequency leads to a drop in the performance of crystal. Characteristics of crystal change as it grows older. It is known as the aging effect of crystal. The Aging effect is triggered by a high drive level and high temperature. Other factors affect the mechanical shock, moisture absorption mounts stress relief. One of the main contributions, the aging effect of crystal is a high drive level due to which frequency deviation is high.

### 2.1.8 Losses

In this subsection, we will be going to discuss the losses in crystal, Losses are due to resistance or real part of the crystal. Depending on where the cut has been made in the equivalent circuit, we can make two distinctive characterizations of the crystal losses. Variation of load capacitance with crystal shown in Fig.2.2[7].

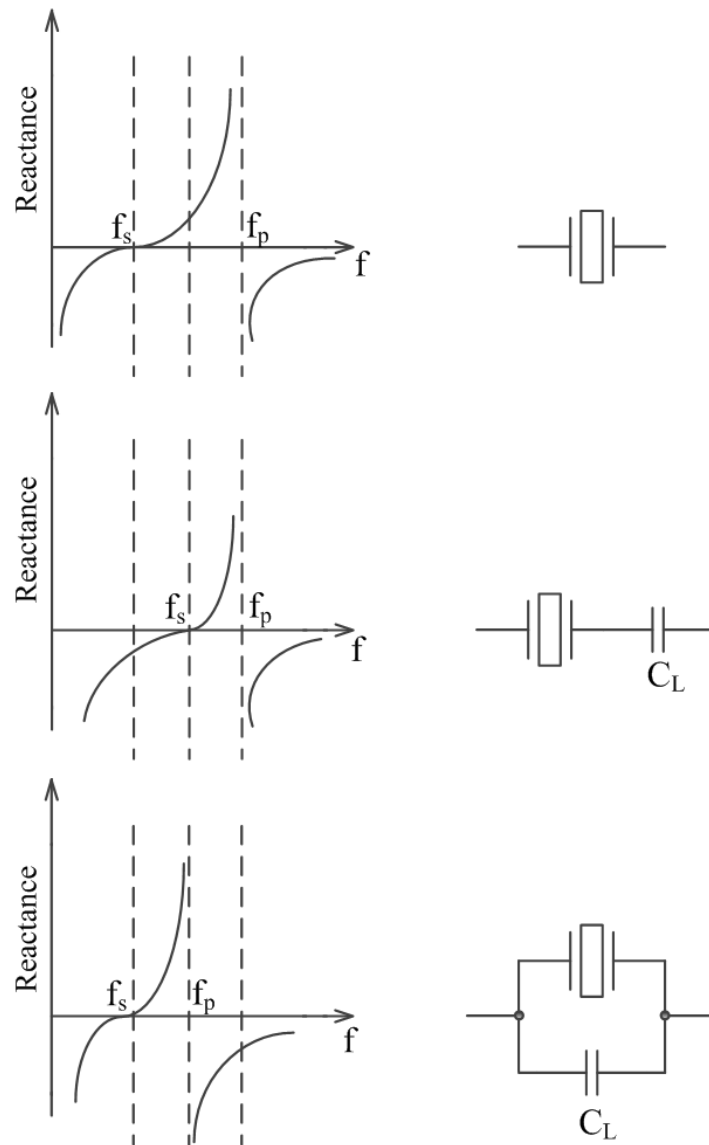


FIGURE 2.2: Load capacitance with crystal

Case (i): The circuit cut's made in Fig.2.3.  $C_0$  and  $C_L$  are considered with the rest of the circuit and we assume  $f_0 = f_s$ :

$$Re(Z_m) = R_m$$

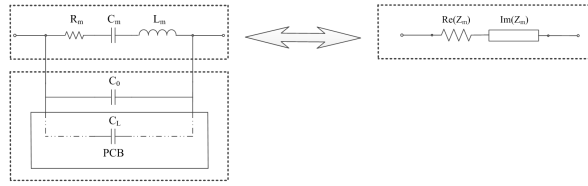


FIGURE 2.3: Crystal Impedance with motional impedance

Case (ii): The circuit cut's made in Fig.2.4. In this case, we can define the equivalent series resistance (ESR) of the crystal:

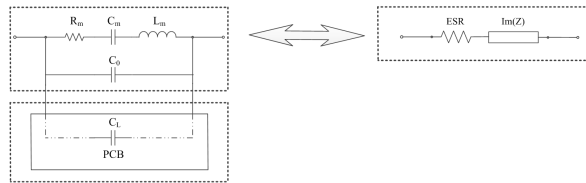


FIGURE 2.4: Crystal Impedance with ESR

### 2.1.9 Drive Level

The drive level of the crystal is due to the power dissipation of the real part of the crystal. Drive level is the level after which the crystal failed to produce oscillation. The main reason is due to excess mechanical vibration. The drive level of the crystal is defined by the frequency and physical size. It is given by a crystal manufacturer. The drive level may cause reversible changes to the crystal. Generally, the drive level is in mW. Power consumed by the crystal is due to drive level and is also known as the power consumption of crystal. The power consumed by an active component of the crystal is known as Equivalent series resistance, ESR [7] i.e:

$$ESR = R_m * \left(1 + \frac{C_0}{C_L}\right)^2$$

The power consumption is given by:

$$P = I_{1,rms}^2 \cdot ESR = \left(\frac{I_{1,P-P}}{2\sqrt{2}}\right) \cdot R_1 \left(1 + \frac{C_0}{C_L}\right)^2$$

Where  $I_{1,rms}$  is the root-mean Square (RMS) value and  $I_{1,PP}$  is the peak-to-peak value of the fundamental signal current.

## 2.2 Related Crystal Oscillator Work

Crystal oscillators are an example of a harmonic oscillator. These oscillators produce sinusoidal wave without giving any input. These oscillators are known as feedback oscillator. They have two subfamilies, first is positive feedback, second is negative resistance which is known as an active element. Positive feedback oscillators follow the Barkhausen model and negative resistance has its model to find out the resistance of the oscillator which is in the inverted current direction. For stable oscillations, one of the necessary conditions is the Barkhausen criterion. Fig 2.5 shows the general model of oscillators. Positive feedback equation has been shown in equ.2.5 & equ.2.6

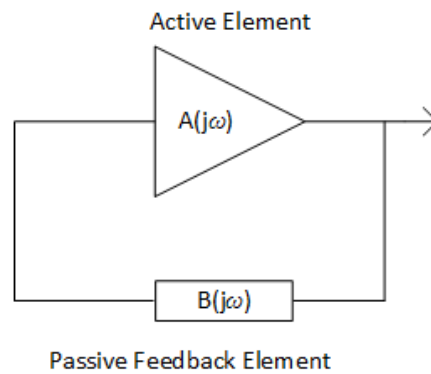


FIGURE 2.5: Feedback Oscillator

$A(j\omega)$  and  $B(j\omega)$  represents feed-forward gain and feedback gain.

Where,

$$|A\beta| = 1, \quad (2.5)$$

$$\angle A\beta = (2N)180^\circ, \quad (2.6)$$

The loop gain of the oscillator are shown in equ. 2.7

$$H(j\omega) = \frac{A(j\omega)}{1 \pm A(j\omega)B(j\omega)} \quad (2.7)$$

### 2.2.1 Negative Resistance

Negative resistance is defined by an applied voltage proportional to applied current which is flowing in the opposite direction. There are two types of branch in the crystal oscillator. Active and passive are two branches in the oscillation loop. Negative resistance model shown in Fig 2.6. Negative resistance is given by an active network, which

is equal to passive branch motional resistance. The Frequency of the crystal is defined when a reactive part of the active branch cancels the passive branch reactive part. The Steady state condition when both branches are equal as follow:

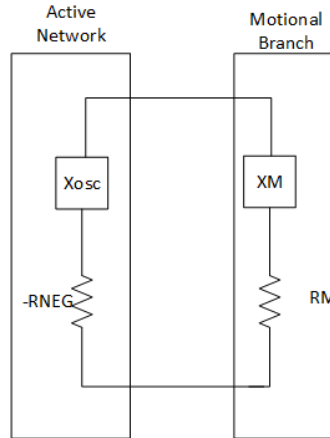


FIGURE 2.6: Negative Resistance Model

$$-R_{NEG} = R_M$$

$$-X_{OSC} = X_M$$

The following Fig 2.7[7] which is an example of the pierce oscillator(a type of a crystal oscillator). To calculate a negative resistance set of equations has been derived.

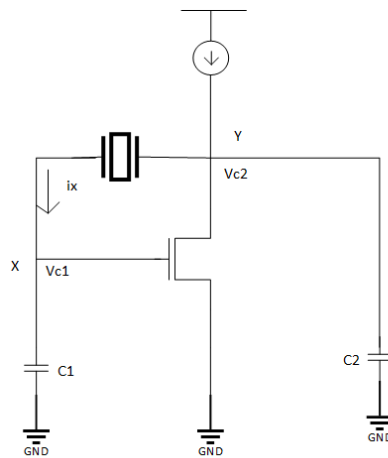


FIGURE 2.7: Pierce Oscillator

$$V_{XY} = V_{C1} - V_{C2},$$

$$X_{C1} = \frac{1}{j\omega C_1}, X_{C2} = \frac{1}{j\omega C_2},$$

$$V_{C1} = i_x * X_{C1} = i_x * \frac{1}{j\omega C_1},$$

$$V_{C2} = -i_x * g_m V_{C1} * \frac{1}{j\omega C_2},$$

$$V_{XY} = i_x * \frac{1}{j\omega C_1} + \left( i_x * g_m \left( i_x * \frac{1}{j\omega C_1} \right) \right) * \frac{1}{j\omega C_2},$$

$$\frac{V}{I} = \frac{1}{j\omega C_1} + \frac{1}{j\omega C_2} - \frac{g_m}{\omega^2 C_1 C_2}$$

$$\text{Imaginary Part} = \frac{C_1 + C_2}{j\omega C_1 C_2}$$

$$\text{Negative Resistance, } -R = -\frac{g_m}{\omega^2 C_1 C_2}$$

### 2.2.2 RF feedback resistor

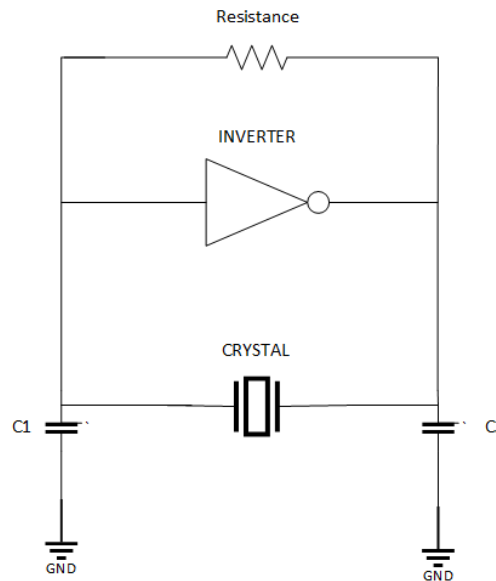


FIGURE 2.8: Cmos Inverter Pierce Oscillator

Fig 2.8[8] shows an example of inverter pierce oscillator (type of crystal oscillator). Resistance over the inverter is called as feedback resistance. Because of this feedback resistance, inverter works as an amplifier. This resistance used to bias the inverter, when  $V_{in} = V_{out}$ , this works in the linear region between  $V_{in}$  and  $V_{out}$  and act as an amplifier. Thermal noise produced between series frequency and parallel frequency of crystal amplified by this amplifier. This will kick start the crystal. After having the stable oscillation on crystal, this feedback resistance can be removed.



### 2.2.3 $C_L$ Load Capacitance

In Fig 2.8  $C_1$  &  $C_2$  known as  $C_L$  load capacitance of crystal. To get the accurate frequency of the crystal load capacitance has been used. Specifications of  $C_L$  is defined by the crystal manufacturer. Both  $C_1$  &  $C_2$  are equal, because  $C_L$  must be constant to provide stable frequency and should be in specification defined by the manufacturer. Mismatch in  $C_1$  &  $C_2$  leads to frequency variation in crystal. The following equation shows the expression of  $C_L$  :

$$C_L = \frac{C_{L1} * C_{L2}}{C_{L1} + C_{L2}}$$

### 2.2.4 Oscillation Transconductance & Allowance

To reach the stable oscillation, crystal oscillator must have enough & sufficient gain. Gain produce by the oscillator transconductance stage will compensate for the losses produced in the loop. It provides enough energy, which starts the oscillator. Due to the presence of passive elements in crystal, which has tolerances, temperature dependency and losses in crystal, which prevent the oscillator to start up. So, the ratio between the oscillator loop gain and oscillator critical gain must be greater than 1. When oscillation is stable, the power produced by the oscillator will be dissipated by the oscillation loop. Two types of transconductance are specified to maintained stable oscillation are the following:

- The minimal transconductance of an oscillator is defined by  $g_{m_{crit}}$ . To maintain stable oscillation, minimal transconductance required. Expression of  $g_{m_{crit}}$  is defined as:

$$g_{m_{crit}} = 4 * ESR * (2\pi f)^2 * (C_0 + C_L)^2$$

Where,

ESR = equivalent crystal resistance,

f = crystal oscillation frequency,

$C_L$  = crystal load capacitance,

$C_0$  = crystal shunt capacitance

- The Oscillator transconductance of an oscillator is defined by  $g_m$ . It is generated by an amplifier stage of the crystal oscillator.

Oscillation allowance is the allowance at which the ratio of  $g_m$  and  $g_{m_{crit}}$  able to produce stable oscillation in the crystal oscillator. It is also known as  $gain_{margin}$ . It is determined

by  $gain_{margin} = g_m/g_{m_{crit}}$ . If  $gain_{margin}$  is lower than 1, oscillation may not be able to build up and this will fail the crystal to start. Hence startup problem arises. Hence greater  $gain_{margin}$  will be required to start the crystal oscillator. Practically,  $gain_{margin}$  of the crystal oscillator must be greater than 5.

### 2.2.5 Startup Time

The time at which, oscillation starts to build and reach a stable state or steady state is known as startup time. Startup state at which addition of the imaginary part of the active, passive device is equal to zero and the sum of the real part of the active and passive gain is less than zero, losses must be canceled. It depends on many factors, for example, ESR,  $C_L$ , Quality factor & gain margin e.t.c. As we discussed in subsection 2.2.4, more gain margin leads to less startup time. Startup time also depends on the quality factor, if the quality factor of the crystal oscillator is high (due to a ceramic resonator) startup time will be high. If ESR will be high, startup time will be high. It also depends on  $C_L$ , if the size of  $C_L$  is higher or lower, discharging time will depend on its size. The startup time at which amplitude grows exponentially is given by the time constant  $\tau$ [6].

$$\tau = \frac{-2L_m}{Re(Z_m) + Re(Z_{osc})}$$

where,

$L_m$  = Motional inductance,

$Re(Z_m)$  = Passive motional resistance,

$Re(Z_{osc})$  = Active gain resistance

## Chapter 3

# Noise & Jitter Analysis

Noise is an undefined signal which is present in the desired signal. It degrades the signal quality & accuracy of an original signal. These signals produced from unknown and random sources. Sometimes the source of the noise is predictable, which can be removable. But non-predictable noise can not be removed. The effect of noise on the device is less, at lower frequencies. At higher frequencies, the impact of noise on the device is more. This device noise degrades the signal quality, which is not acceptable. Hence, it is important to characterize the noise at a high RF frequency. Noise can be broadly classified into two parts.

1. Extrinsic noise
2. Intrinsic noise

### 3.0.1 Extrinsic Noise

Extrinsic noise of the signal is generated by the source inferred from external sources. This external noise generated from the nearby environment. Due to unpredictable sources e.g. power supply, parasitic, external parameters, crosstalk, and electromagnetic interference are the source of extrinsic noise. This noise can be compensated or reduced by reducing the noise power or strengthening the signal power. This will improve the (SNR) signal to noise ratio.

### 3.0.2 Intrinsic Noise

The noise which is created inside the device is known as intrinsic noise. The noise created by the device can be predicted up to a certain extent. Sources of the noise are due to variations in process, voltage, temperature, variation in capacitance, gate

tunneling and mobility variations e.t.c. Nowadays, due to scaling in technology most of the designs contain more intrinsic noise because of increment in technology variation, due to less device spacing. By reducing the power optimization techniques this noise can be compensated. By using the optimized layout techniques fundamental noise can be reduced.

### 3.1 Types of Intrinsic Noise

There are several types of fundamental noise in CMOS device, This noise occurring at various terminals and active regions of the MOS device. They are thermal noise, shot noise, flicker noise, generation-recombination noise, and substrate noise.

#### 3.1.1 Thermal Noise

Thermal noise is a type of intrinsic noise. Thermal noise is produced due to thermal fluctuations of an electron inside the conductor. It is also known as Johnson-Nyquist noise. Thermal noise occurs due to random change in direction of a thermal electron which is also known as Brownian motion. Thermal noise produced inside the device, it is impossible to identify the effect of current and voltage noise produced due to its random nature. Thermal noise measured statically due to its random nature. In a CMOS device, the thermal noise of a resistor modeled by the following noise voltage equation & current equation:

$$\overline{V_n^2} = 4kTR\Delta f$$

$$\overline{I_n^2} = 4kT\gamma g_m$$

Where,

k = Boltzmanns constant,

T = Temperature of the device,

$\Delta f$  = range of frequencies,

R = Resistance,

$g_m$  = transconductance of mos device

The power spectral density is independent of resistance material. It is dependent on absolute temperature. Thermal noise is produced inside the channel of nMOS and pMOS transistor. This noise does not vary much concerning a change in frequency for practical applications. Hence, Thermal noise is a very dominant noise in RF applications. This is also is known as "White noise".

### 3.1.2 Shot Noise

When electrons and holes cross the potential barrier in the transistor, This produces the shot noise. These potential barriers are found at the junction depletion region, channel depletion region in a CMOS device transistor. In the time domain, the current is the sum of discrete pulses. The Current noise is proportional to temperature. Hence, by lowering the temperature shot noise can be reduced.

### 3.1.3 Flicker Noise

Flicker noise is also called 1/f noise. Frequency is inversely proportional to the power density of electronic devices. The main mechanism of flicker noise still under investigation its exact mechanism and origination are uncertain and unknown. But, different models suggest that it generates from the oxide traps which traps and release in the channel. It has been suggested that it is generated from source, bulk, dangling bonds, silicon interface. It has been found that for different devices, flicker noise has been different.

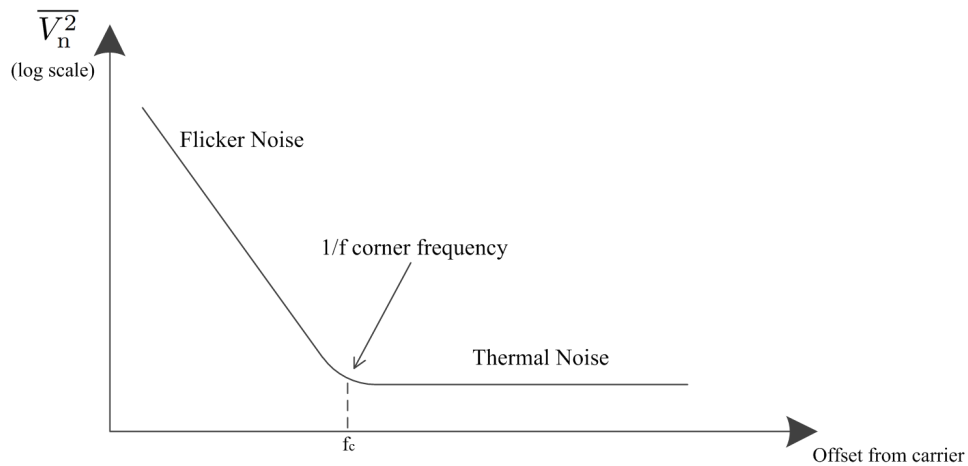


FIGURE 3.1: corner frequency 1/f

Flicker noise has been generated from defects present at the surface and it can be modeled easily, these defects depend on the fabrication of CMOS technology. Flicker noise is lesser in PMOS than NMOS, because holes in PMOS keep the distance from these traps. Flicker noise in CMOS devices can be modeled by a voltage source in series with the gate or current source connected between drain and source. They are given by

$$\overline{V_n^2} = \frac{K}{WLC_{ox}} \frac{1}{f_m}$$

$$\overline{I_n^2} = g_m^2 \frac{K}{WLC_{ox}} \frac{1}{f_m}$$

Where,

W is the gate width,

L is the channel length,

$C_{ox}$  is the gate oxide capacitance per unit area,

K is a constant

Fig.3.1[9] shows the flicker noise & thermal noise at which power spectral density of thermal frequency  $1/f$  intercepts at  $f_c$  is known as corner frequency. By equating the flicker and thermal noise, corner frequency  $f_c$  at  $1/f$  can be calculated[7].

$$g_m^2 \frac{K}{WLC_{ox}} \frac{1}{f_m} = 4kT\gamma g_m \Leftrightarrow f_c = \frac{K}{WLC_{ox}} \frac{g_m}{4kT\gamma}$$

### 3.1.4 Generation – Recombination noise

The Generation-Recombination noise is generated due to fluctuations in free carriers with random charge carriers in different energy bands. This will cause a fluctuation in current flow. It represents a typical noise that depends on the carrier concentration of semiconductors material. The generation-recombination noise in MOS devices originates from bulk silicon defects. These defects create traps that capture or release carriers. Recombination noise is caused by these trapping centers in the bulk of the device. Generation recombination noise in MOS is usually much smaller than  $1/f$  noise.

### 3.1.5 Substrate noise

The noise produced through the substrate of a transistor is known as substrate noise. In between drain, source and substrate virtual capacitors formed between the bulk, drain or sources region. These capacitors only affect the high frequency, a small current will pass through the bulk of the mos device because at high-frequency capacitors act as short and it allows this leakage current. Lower frequency does not have any effect on these capacitors at lower frequency capacitors act as an open. The following equation shows the substrate noise dependency on the frequency with resistance.

$$f_{max} = \frac{f_t}{2} \sqrt{\frac{r_{out}}{R_s}}$$

The substrate noise affects the output resistance and output conductance of the device. Frequency increases the output resistance will also increases, which leads to more substrate noise. Most dominating noise is thermal noise as it tends to affect the wide range of frequencies.

## 3.2 Oscillator Noise

Oscillator oscillates at its fundamental frequency which is  $f_0$ . It produces sinusoidal frequency. While converting into the frequency domain, sinusoidal frequency converts into two Dirac delta function centered at frequencies  $-f_0$  and  $f_0$ . If the oscillator is ideal, all the energy distribute over this frequency. Practically, the oscillator has some amount of energy distribute or spread around the oscillation centered frequency, which is known as phase noise. Phase noise is the combination of noise discussed in the above subsection thermal, shot, flicker, generation- recombination and substrate noise and extrinsic noise. Oscillator amplitude has a maximum and minimum limit at which it oscillates. The amplitude of the oscillator is controlled by the non-linearity in the circuit. The amplitude and loop gain of the oscillator is inversely proportional to each other. If amplitude decrease, loop gain increases or amplitude increases, loop gain decreases. If there is a change in the phase of the oscillator, then is no loop restoring force. Hence phase noise became the critical aspect of an oscillator.

### 3.2.1 Phase Noise In Oscillator

Phase noise or jitter are two important parameters of an oscillator. They have a direct impact on the performance of a system. Noise can corrupt a signal, it can change the frequency spectrum & timing spectrum of the signal. Phase noise and jitter are associated with the noise of an oscillator. Phase noise is defined as the fluctuation in the frequency output of an oscillator. It is due to the random change in the phase of an oscillator. At frequency domain, due to intrinsic and extrinsic noise, the phase at the central frequency of an oscillator changes from its original phase to an unwanted phase of an oscillator. The Phase noise of an ideal and practical oscillator has been shown in Fig.3.2. Ideally, an oscillator output must be pure sinusoidal, it must be Dirac delta in frequency domain represented as a vertical line at a single frequency. However, in practice, due to the noise source inside an oscillator, the output of an oscillator changes to its original position near its carrier frequency. The output of an ideal and real oscillator mathematically expressed as follows:

- Output of an ideal oscillator:  $V_0 = A_0 \sin(\omega_0 t)$

- Output of a real oscillator[10]:  $V_0 = A_0(1 + A(t) \sin(\omega_0 t + \phi(t)))$

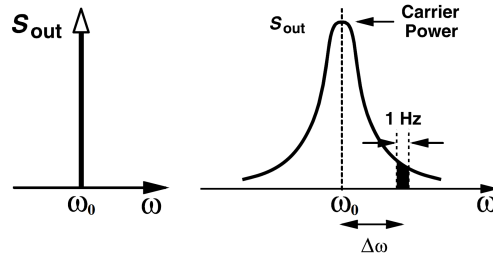


FIGURE 3.2: Phase noise of an ideal and practical oscillator

Where,  $A_0$  is the amplitude of an oscillator signal,  $\omega_0$  is the frequency of an oscillator,  $A(t)$  is amplitude fluctuation of an oscillator,  $\phi_t$  is phase fluctuation of an oscillator.

### 3.2.2 Phase Noise Curve

Phase Noise of practical oscillator is measured as the ratio of noise power and the carrier around 1Hz bandwidth at a specified frequency as shown in Fig.3.2. It is also specified as dBc/Hz at a given offset frequency, whereas dBc is known as noise power to the carrier at specified frequency in a logarithmic scale. Equ3.1 shows the phase fluctuations of a real oscillator in terms of power spectrum density :

$$S_\phi(f) = a_0 + a_1 f^{-1} + a_2 f^{-2} + a_3 f^{-3} + a_4 f^{-4} \tag{3.1}$$

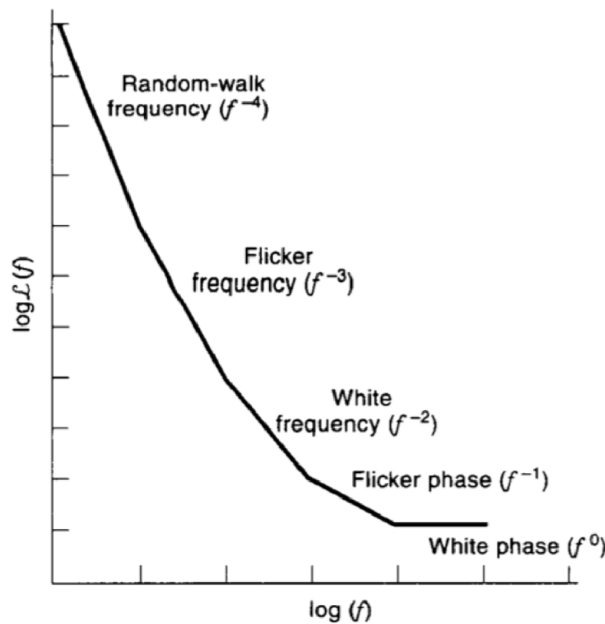


FIGURE 3.3: Phase Noise Model



The different components of noise have been defined by the coefficient of a & shown in equ.3.1. The slope of the single-sideband phase noise,  $L_\phi(f)$  is defined by the defined spectrum degree frequency. As shown in Fig.3.3[11] spectrum degree with 0, -1, -2, -3, -4 usually named as White phase modulation PM (WHPM), Flicker (FLPM), Random Walk PM (RWPM) also known as White Frequency Modulation (WHIFM), Random Run PM (RRPM or Flicker FM (FLFM)), and Random Walk (RWFM). Along with the reduction of  $f_m$ , a strong effect of the short-term noise of  $L_\phi(f)$  appears. Closer the frequency to the carrier, the larger  $S_\phi(f)$  is. Extremely  $S_\phi(f)$  will reach infinite. But in the real circuits, it is not efficient that all components of  $S_\phi(f)$  are presented. Each component comes out only in the specific frequency range.

### 3.2.3 Leeson's Phase Noise Model

The phase noise of an oscillator is described by an equation which is given by David B. Leeson. Phase noise, Leeson model equation is given by[9]:

$$L(\Delta\omega) = 10\log\left(\left[\frac{2FkT}{P_{sig}}\right]\left[1 + \left(\frac{\omega}{2Q\Delta\omega}\right)^2\right]\left[1 + \frac{\Delta\omega_{1/f^3}}{\Delta\omega}\right]\right) dBc/Hz \quad (3.2)$$

Where,

$P_{sig}$  = oscillator output power,

$\Delta\omega$  = offset from the oscillation frequency,

$L(\Delta\omega)$  = single sideband phase noise density,

F = active device noise factor,

$\Delta\omega_{1/f^3}$  = break between 1/f flicker noise and a frequency range with slope 20 dB/decade.

Fig.3.4[9] shows Lesson phase noise model. Shot noise & thermal noise & dominates, region between the  $\Delta\omega/2Q$  and  $\Delta\omega_{1/f^3}$ . 1kHz region lies behind  $\Delta\omega_{1/f^3}$ .  $\Delta\omega/2Q$  lies around in the few MHz region. As shown above in lesson noise model equ.3.2, Phase noise of an oscillator can be reduced:

- The power dissipated by the oscillator and quality factor of an oscillator is directly proportional to the carrier to noise. To reduce the phase noise or noise around the carrier, the quality factor of the oscillator should be increased.
- It can be reduced by increasing the width and length of the device. This will reduce the flicker noise. If the devices used for the oscillators have less device noise, the phase noise of an oscillator can be improved. If the noise floor can be

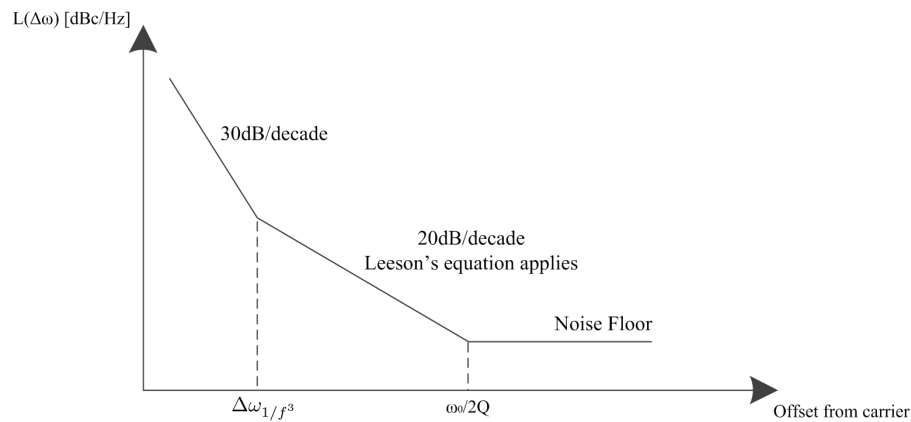


FIGURE 3.4: Leeson's Phase Noise Model

moved further due to less intrinsic noise, at lower offset frequency noise will get improved.

- It can be reduced by reducing the current consumption of a signal. The power of the signal reduced, due to reduced current consumption. This will reduce the phase noise of an oscillator.

### 3.3 Timing Jitter in Oscillator

Jitter is defined as short-term variations of the significant instants of a signal from their ideal positions in time and essentially describes how far the signal period has deviated from its ideal value. Jitter is a variation in the zero-crossing times of a signal or a variation in the period of the signal. Jitter is often defined as an RMS quantity. Jitter is composed of two major components, one that is predictable and one that is random. The predictable component of jitter is called deterministic jitter. The random component of jitter is called random jitter. Random jitter comes from the random phase noise, while deterministic jitter comes from the deterministic noise[11].

#### 3.3.1 Random Jitter

Random Jitter is uncorrelated jitter and describes timing variations caused by less predictable influences. Random jitter is characterized by a Gaussian distribution and assumed to be unbounded. It can be caused by many sources, such as thermal or other physical, random processes. These sources include are shot noise, thermal noise, flicker noise[10].

### **3.3.2 Deterministic Jitter**

Deterministic jitter is created by identifiable interference signals. It is always bounded in amplitude, has Specific (not random) causes, and cannot be analyzed statistically. It is caused by many sources such as crosstalk between adjacent signal traces, EMI radiation on a sensitive signal path, Noise from power layers of a multi-layer substrate and simultaneous switching of multiple gates to the same logic state.

## Chapter 4

# Proposed Architecture Design

This chapter discusses the proposed crystal oscillator design with the proposed transconductance stage along with all blocks. This crystal oscillator is designed to produce a 25MHz clock with low phase noise and fast startup.

### 4.1 Proposed System Architecture

Table.4.1 shows the specification required to design crystal oscillator. Fig.4.1 shows the proposed functional block diagram. The crystal oscillator starts when digital logic starts working. This logic starts the gm stage (current stage & stage 1-7). Now, gm stages provide sufficient gain and current to crystal. As discussed above in subsection 3.1.9 that currently given to crystal must not exceed the drive level of crystal and minimum current must provide, so that the crystal starts its functionality. Due to sufficient gain and current, the crystal starts to resonate at its fundamental frequency. Oscillation starts to build slowly, at a certain time interval at which stable oscillation achieved, also

TABLE 4.1: Specification

<b>Technology</b>	TSMC 28nm
<b>Supply 1</b>	1.8V (1.6V to 2.0V)
<b>Supply 2</b>	0.9V (0.8V to 1.0V)
<b>Crystal Frequency</b>	25MHz
<b>Output clock</b>	0 to 0.9V
<b>Load Capacitor</b>	10pF
<b>Drive Level</b>	$\leq 200\mu\text{W}$
<b>Startup Time</b>	$\leq 1\text{ms}$
<b>Phase Noise @1kHz</b>	$\geq -120\text{dBc/Hz}$
<b>Phase Noise @1MHz</b>	$\geq -150\text{dBc/Hz}$
<b>Jitter @<math>\geq 1\text{MHz}</math></b>	10ps

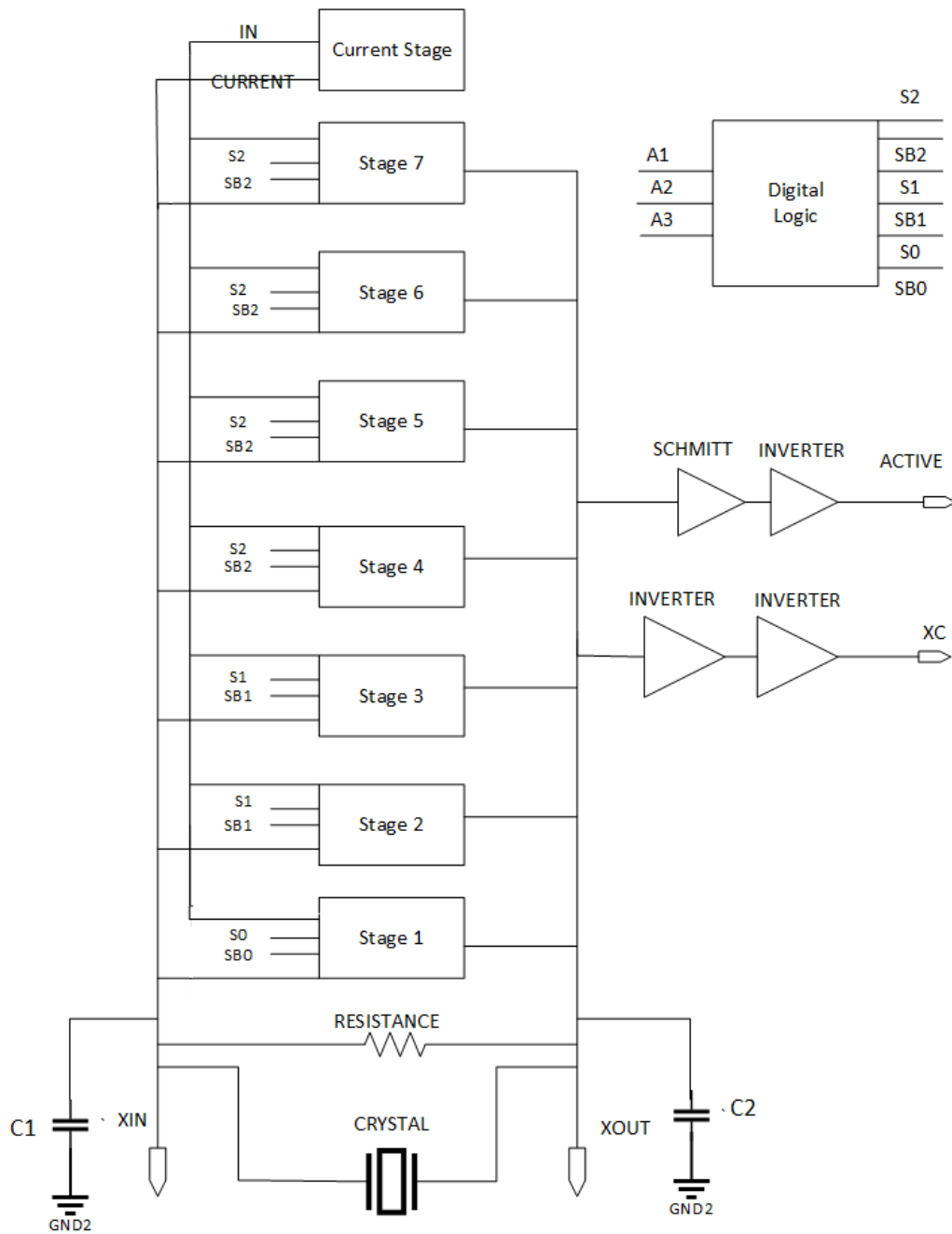


FIGURE 4.1: Proposed Architecture of Crystal Oscillator

called as startup time. These sinusoidal oscillations can be converted to a square wave pulse by the use of CMOS buffer[12] and Schmitt trigger[13].

## 4.2 Digital Logic

Digital logic consists of a combination of NAND gates and level shifters shown in Fig.4.2. Operation starts at an active mode when A1, A2, A3 and reset is at high logic 1. This logic pass through the NAND gate which gives logic '0' to the input of level shifter shown in Fig.4.3. Due to positive feedback present in the level shifter. It converts the input logic '0' to output Out port to logic '1' & output Outb port to logic '0'. Which gives SB0, SB1, SB2 go to logic 0, and S0, S1, S2 go to logic 1. Standby mode, when only A3 and reset is at logic '1' others at logic '0'. S2 and SB2 go to logic '1' & '0'. S1,S0 and SB1, SB0 go to logic '0' & '1' respectively.

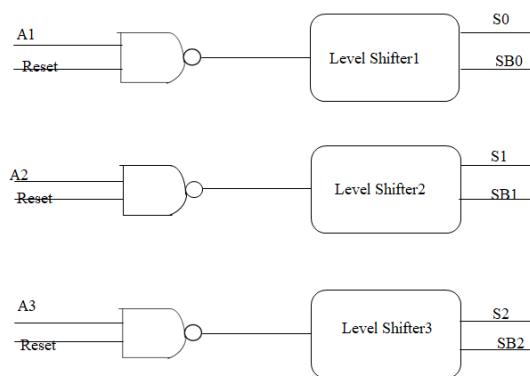


FIGURE 4.2: Digital Logic

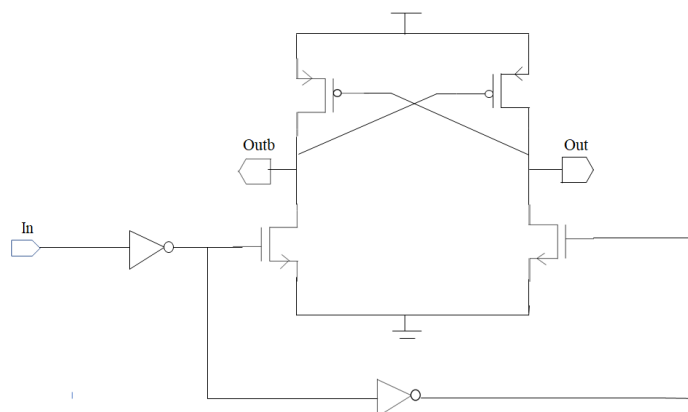


FIGURE 4.3: Level Shifter

### 4.3 Related Gm Stage

There are many traditional gm stage circuits for crystal oscillator, which are widely used in the industry for crystal oscillator. Some of them are discussed here. In this section, Some of the existing Gm stage techniques have been discussed.

#### 4.3.1 Pierce Inverter Gm Stage

There are many traditional gm stage circuits for crystal oscillator, which are widely used in the industry for crystal oscillator. Pierce-Gate oscillator (Inverter based crystal oscillator) shown in Fig.4.4[14] is very popular as a topology that minimizes the tank loading minimizing the crystal de-Qing and consumes less power compared to the other topologies, the configuration is not robust and stable with Process, Voltage and Temperature variations (PVT).

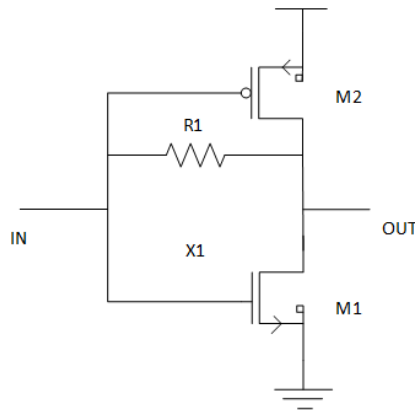


FIGURE 4.4: Inverter Gm stage

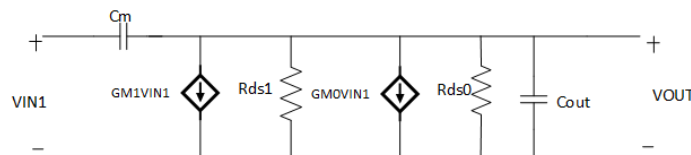


FIGURE 4.5: Small signal model of Inverter Gm stage

$$Gain = \frac{V_{OUT}}{V_{IN1}} = \frac{-(G_{M1} + G_{M0})}{G_{ds1} + G_{ds0}}, R_0 = \frac{1}{(G_{dsM1} + G_{dsM0})}$$

These can significantly degrade the Phase Noise (PN) and Power Supply Rejection Ratio (PSRR) performance, as well as the output frequency stability, one of the most important parameters when designing crystal oscillator. Moreover, if the Transconductance of

the sustaining amplifier varies significantly with PVT, the oscillator could even fail to oscillate.

### 4.3.2 Class AB Gm Stage

This configuration has more robust and stable with Process, Voltage and Temperature variations (PVT) than an inverter-based crystal oscillator. Class AB gm Stage circuit is shown in Fig.4.6 needs an extra biasing circuit to bias M2 which introduces extra complexity.

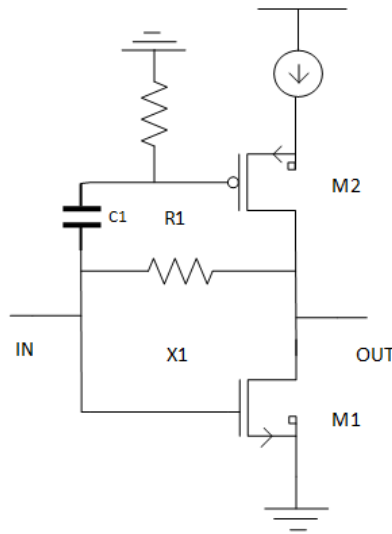


FIGURE 4.6: Class AB Gm Stage

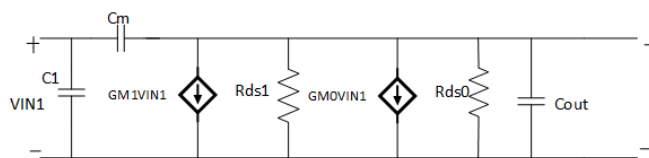


FIGURE 4.7: Small signal model of class AB Gm Stage

Small signal analysis results:

$$Gain = \frac{V_{OUT}}{V_{IN1}} = \frac{-(G_{M1} + G_{M0})}{G_{ds1} + G_{ds0}}, R_0 = \frac{1}{(G_{dsM1} + G_{dsM0})}$$

The area of the overall circuit increases, due to extra biasing circuit addition in the overall architecture. This extra biasing circuit consists of diode-connected NMOS and PMOS, which has PVT variation. This architecture has better phase noise than the inverter-based crystal oscillator. If, the power supply of both architectures is the same



as voltage sinusoidal swing rail to rail of this architecture is less than the previous architecture. Due to lower rail to rail swing, power consumption is lower than the previous architecture. It has more startup time than the other previous architecture, because of the extra capacitor attached to the crystal.

#### 4.4 Proposed Gm Stage

To mitigate the above-stated limitations of the gm stage. Gm boosting loop has been proposed which consist of current stage shown in Fig.4.8 and its gain stage shown in Fig.4.9. A Combination of current and gain stage leads to increment in gain and amplitude as compared to the inverter and class AB push-pull gm stage. This configuration has more robust and stable with PVT variations than the other architectures. This architecture does not need extra bias circuit. This architecture has a full rail to rail swing. This architecture can track and control the current consumption at input and output.

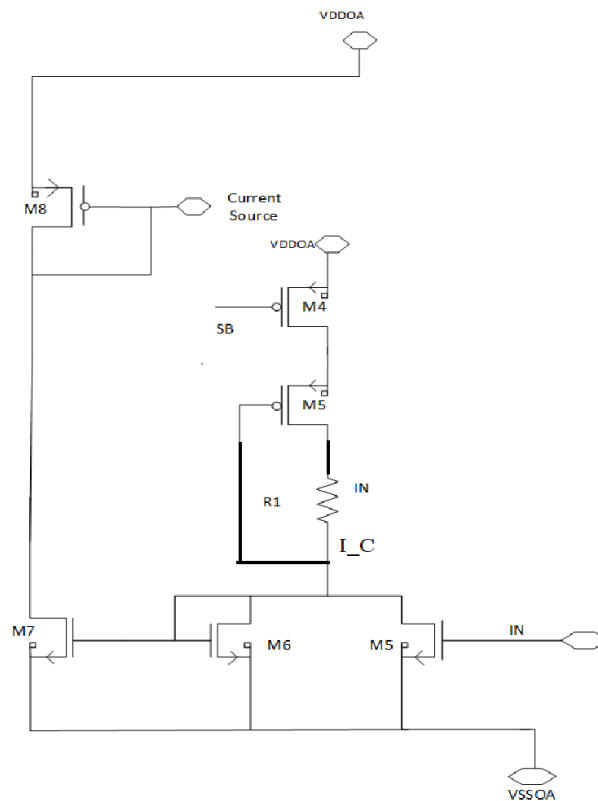


FIGURE 4.8: Proposed Gm Current stage architecture

In the proposed Gm current stage, When SB goes to zero, R1 and diode-connected PMOS (M5) passes the current, these currents divided into two parts NMOS (M5, M6). So, whenever the current tries to go more into NMOS (M6) than other current tries to pull it back to NMOS (M5). This operation leads to compensate for current consumption so it has less effect on PVT variation.

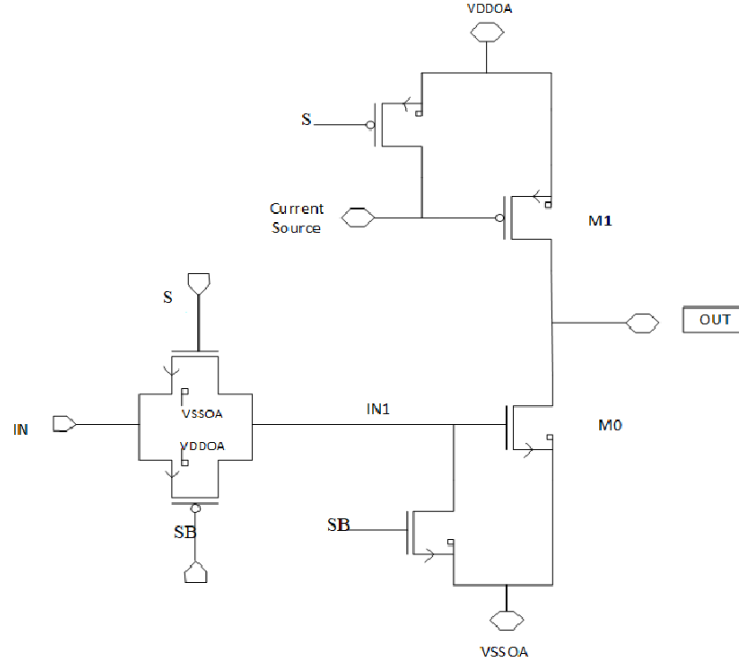


FIGURE 4.9: Proposed Gm gain stage architecture

In the proposed Gm gain stage, current stage PMOS (M8) current mirrors to PMOS (M1). This stable current flows into the NMOS (M0). Due to which, Common mode maintains between PMOS (M1) & NMOS (M0). Hence, the duty cycle of this architectures is best. This gain stage gives the fast startup time because the gain of the architecture depends on the multiplication of transconductance NMOS (M0) and resistance of PMOS (M1) & NMOS (M0). The proposed Gm stage improves the phase Noise & jitter of the oscillator.

Gain equation of the proposed Gm stage:

$$A = A_0 \left[ \frac{1 - \frac{s}{z}}{1 + \frac{s}{p}} \right]$$

Small signal analysis and gain of the proposed Gm stage:

$$A_0 = \frac{V_{OUT}}{V_{IN1}} = \frac{-G_{M0}}{G_{ds1} + G_{ds0}} = -G_{M0}R_0$$

Gain Bandwidth equation derivation:

The impedance of  $C_{gd}$  and  $C_{db}$  capacitors of the devices are very large compared to the impedance offered by  $C_{OUT}$

$$R_0 = \frac{1}{(G_{dsM1} + G_{dsM0})}, z = \frac{-G_{M0}}{C_{gdM0} + C_{gdM1}}$$

$$C_0 = (C_{gdM0} + C_{gdM1} + C_{dbM0} + C_{dbM1} + C_{OUT})$$

$$p = -\frac{(G_{dsM1} + G_{dsM0})}{(C_{gdM0} + C_{gdM1} + C_{dbM0} + C_{dbM1} + C_{OUT})} = -\frac{1}{R_0 C_0} \simeq -\frac{(G_{dsM1} + G_{dsM0})}{C_{OUT}}$$

This is a single pole system because zero occurs at a very high frequency. Gain Bandwidth Product(GB) and is given by

$$GB = A_0 * p = -G_{M0}R_0 * \left( -\frac{1}{R_0 C_0} \right) = \frac{-G_{M0}}{C_0}$$

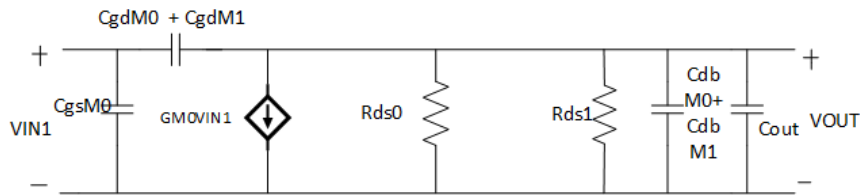


FIGURE 4.10: Small signal model of proposed Gm stage architecture

## 4.5 Buffer Stage

There are many ways to convert the sinusoidal wave to a square wave. One of the easiest ways is to use a CMOS buffer shown in Fig.4.11[15]. The CMOS buffer consists of two back to back inverters. The size of the second inverter increases by 3x, 7x to drive the buffer capability. Reduced power supply and sub-threshold voltage, these buffers are more vulnerable to noise reduced power supply and noise robustness. Due to these

supply variations and PVT variation occurs these buffer may not able to give a better duty cycle. These variations lead to false stabilize output. To improve the output stabilization, The Schmitt trigger can be used. Another way is to increase the length & width of the transistor, which leads to an increase in the area.

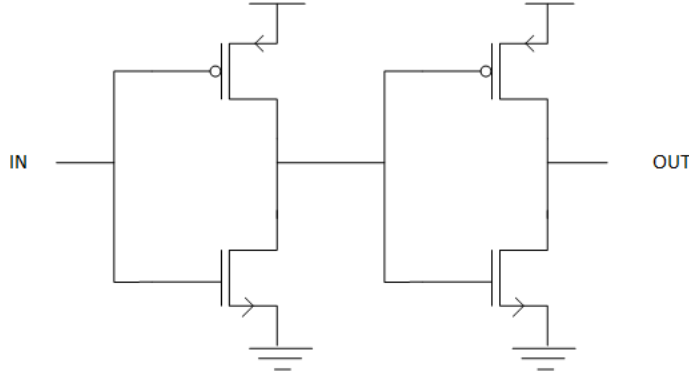


FIGURE 4.11: Buffer Stage

## 4.6 Schmitt Trigger Stage

CMOS buffers are limited to supply variation and noise robustness, one of the ways to improve is to use Schmitt trigger design shown in Fig.4.12[15]. These are the positive feedback circuit in which loop gain of this circuit is greater than one. Because of the feedback present in the circuit, it stabilizes the output logic and reduces sensitivity to noises. The input of these circuit changes below/above a predefined threshold level, due to feedback output logic holds its value and undesired noise not able to trigger a change at the output. This Schmitt trigger design consists of an inverter (M2, M1) and two more pairs of PMOS (M2, M5) & NMOS (M0, M5). These two pairs of NMOS and PMOS are used to provide positive feedback at logic low & high. When  $V_{in} < V_{th_{nmos}}$ ,  $V_{out} = V_{DD}$ , and M4 is in saturated and on, both M0 & M1 are off. When  $V_{in} > V_{th_{nmos}}$ , M0 became on whereas M1 remains off due to the present feedback voltage at its drain terminal. This feedback voltage depends on the dimensions of M0, M4 and  $V_{th_{nmos}}$ .

$$V_{FB} = V_{DD} - V_{THN} - (V'_{IN} - V_{THN}) * \sqrt{(W_{N1} * LN2)/(W_{N2} * LN1)}$$

where L and W are the corresponding transistors length and width.  $V_{FB}$  improves the SNM of the ST-INV since a higher  $V_{NOISE}$  is now required for switching N0 on ( $V'_{IN} = V_{THN} + V_{FB}$ ). Therefore, the high switching threshold becomes :

$$V'_{IN} = V_{THN} + (V_{DD} - V_{THN}) * (1 + \sqrt{(W_{N1} * LN2)/(W_{N2} * LN1)})^{-1}$$

Assuming that N1 and N2 have the same dimensions, the high switching threshold is  $(V_{DD} + V_{THN})/2$ . Similarly, in case of pMOS transistors, the ST-INV low switching threshold is:

$$V'_{IN} = V_{DD} - V_{THP} + (V_{DD} - V_{THP}) * (1 + \sqrt{(W_{P1} * LP2)/(W_{P2} * LP1)})^{-1}$$

Assuming that P1 and P2 have the same dimensions, the low ST-INV switching threshold is improved to  $(V_{DD} - V_{THP})/2$ .

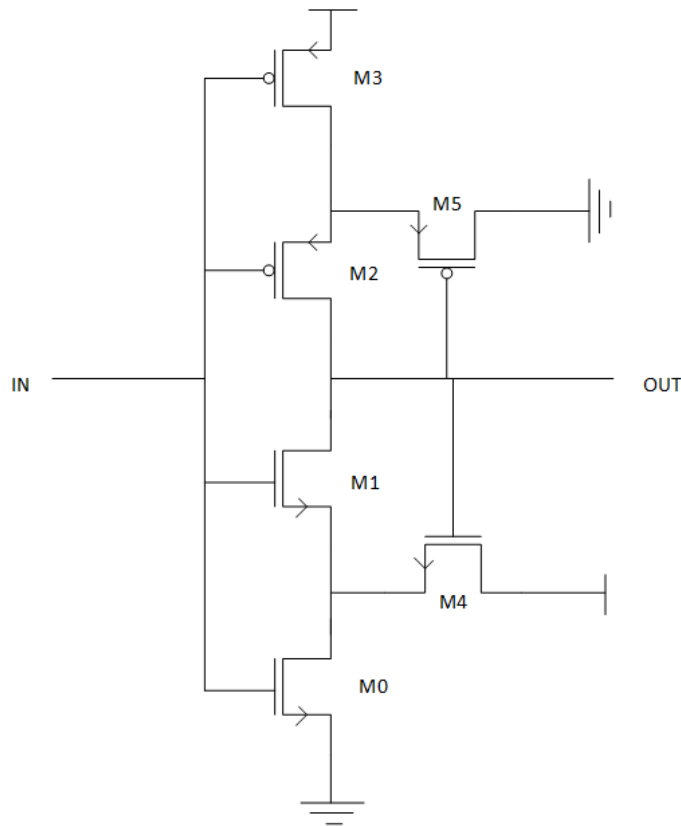


FIGURE 4.12: Schmitt Trigger

## Chapter 5

# Result and Discussion

This chapter presents the simulation results of the proposed crystal oscillator and transconductance stage. The circuits are implemented in Cadence Virtuoso TSMC 28nm CMOS technology and simulations took place using the HSPICE & SPECTRE simulator. The characterization has been done on basis of many variables such as outer supply voltage variation from 0.8v to 1.0v, inner supply voltage variation from 1.6v to 2.0v, temperature variation from -40C to 125C, resistance and capacitance variation up to (45%), MOS parameters mismatch is taken up to  $3\sigma$ . Other variations could be due fabrication process variation such as  $V_{th}$  and  $C_{ox}$  variation. Simulations have been performed for cross corners with variation in MOSFET intrinsic parameters, temperature, and resistance. Process corners are used for simulations are Typical, Fast Fast(FF), Fast Slow(FS), Slow Fast(SF) and Slow Slow(SS). A total of 45 corners is being used for the simulation of the proposed crystal oscillator.

### 5.1 Dc Analysis

This section contains the Dc analysis of the proposed transconductance stage of the crystal oscillator. Dc analysis shows the operating point of the circuit. In this case, the Dc analysis shows the operating point of the gm stage. As input varies from 0 to 1.8v, and supply varies from 1.6v to 2.0v, the output characteristic of the transconductance stage works as an amplifier input region between 0.7v to 1.1v. This region is in the linear region as we discussed earlier in chapter 3. The input region between 0v to 0.6v gives full supply voltage at the output, the input region between 1.2v to 1.8v output goes to ground voltage. While doing the dc analysis, it has been found one gm stage producing  $200\mu A$  current at a Typical corner. 30% gm stage current variation has been

found out at cross corners. At cross corners, all gm stages (30-35)% current variations have been found out.

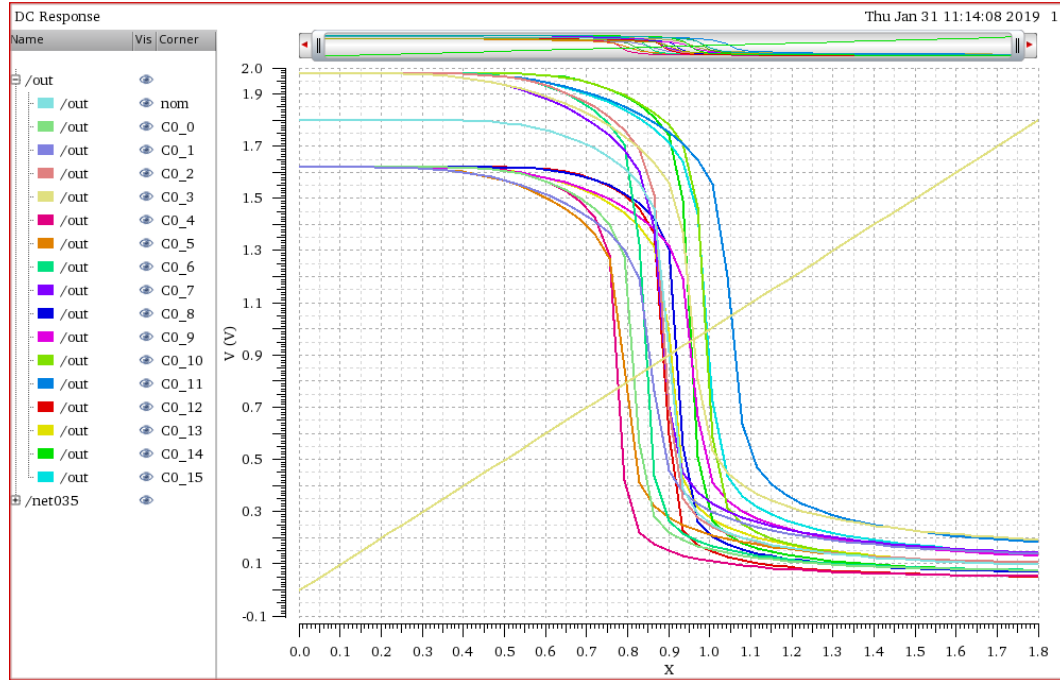


FIGURE 5.1: Dc Sweep

## 5.2 Open Loop Analysis

This section contains the open loop analysis of the proposed transconductance stage of the crystal oscillator. Open loop analysis has been done by a loop break technique. In Fig 5.1, disconnect the crystal, then a 0V voltage source is placed in series in the loop, one pin of the voltage loop connected to the loop input, the other pin to output pin. Open loop stability analysis has been presented by using the cadence spectre.

Fig.5.2, represents open loop analysis of proposed crystal oscillator gm stages at PVT variations. When all 7 gain stages are connected then gain achieved at the typical corner is 15.14dB at the frequency of 25MHz. The phase margin of the gm stages at the typical corner is  $94.4^\circ$  at the frequency of 25MHz. Gain @25MHz varies from 19.17dB to 11.7dB. Phase @25MHz varies from  $101^\circ$  to  $94.4^\circ$ . At the low power mode, when only 4 gm stages are connected. At PVT corners, Gain @25MHz from 15.1dB to 7.761dB. At PVT corners, phase @25MHz from  $87.81^\circ$  to  $97.56^\circ$ .

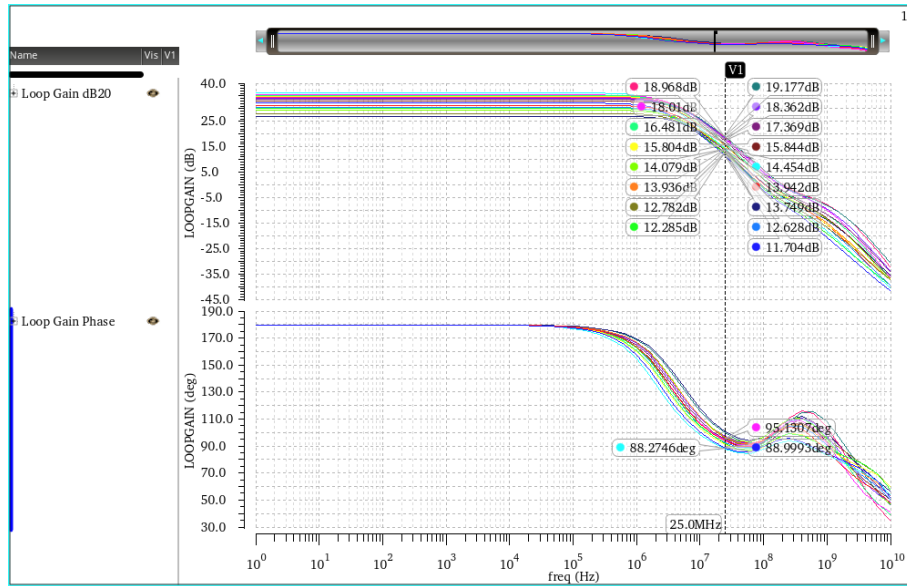


FIGURE 5.2: Open Loop Stability Analysis

### 5.3 Closed loop Ac Analysis

This section contains the closed loop ac analysis of the proposed crystal oscillator. Closed loop analysis has been done by maintaining the loop. When crystal connected with all the gm stages. Ac signal has been applied between Xin and crystal, then stability analysis has been performed. Fig.5.3 represents the closed loop analysis results when all the gm stages connected to the crystal at PVT corners.

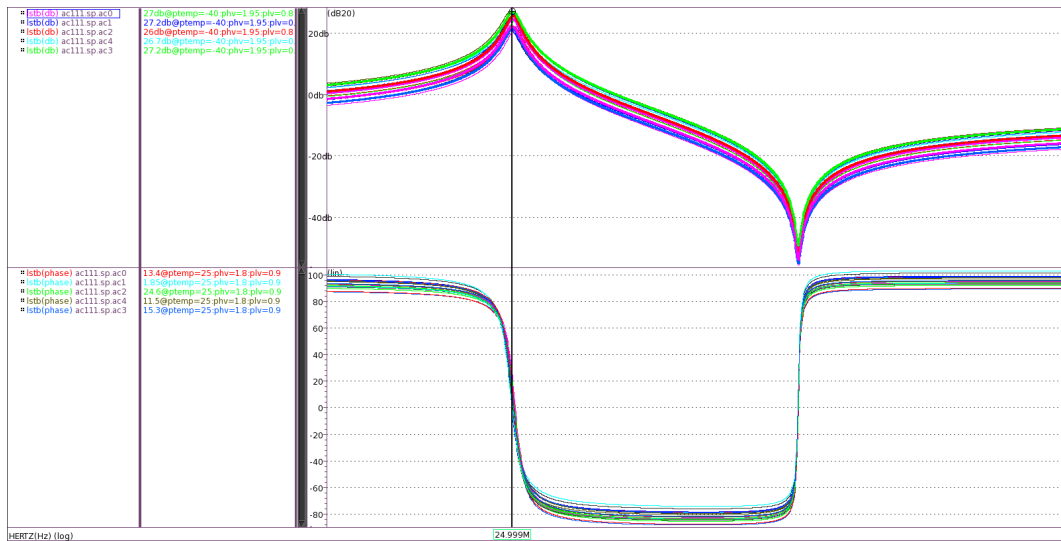


FIGURE 5.3: Closed Loop Ac Analysis

At the series resonant frequency, L1 and C1 cancel, impedance is determined by R1. The second higher frequency is the parallel resonant frequency. At parallel resonance, resistance is at a maximum. A typical corner gain @25MHz is 24.7dB, the total phase



is  $174.7^\circ$ . At PVT corners the closed loop gain has been varied from 27.3dB to 21.2dB. At PVT corners the closed loop phase has been varied from  $165^\circ$  to  $176^\circ$ . At the low power mode, when only 4 gm stages are connected. At PVT corners, Gain has @25MHz from 24.9dB to 17.5dB. At PVT corners, phase @25MHz from  $164^\circ$  to  $175^\circ$ .

## 5.4 Transient Analysis

This section contains the transient analysis of the proposed crystal oscillator. Transient analysis has been performed in the HSPICE simulator. Fig.5.4 shows the transient result of the proposed crystal oscillator at a typical corner. Fig.5.5 shows the zoomed view of transient result. When all 7 gm stages(active mode) are connected to crystal, the crystal starts to resonate at 25MHz. The startup time of the crystal oscillator at the typical corner is 120u. At PVT corners, the startup time of the crystal is varied from 120u to 136u. While performing the transient analysis, current consumption at the inner supply has been found out at a typical corner is 789uA. At PVT Current consumption at supply varies from 520uA to 1.58mA.

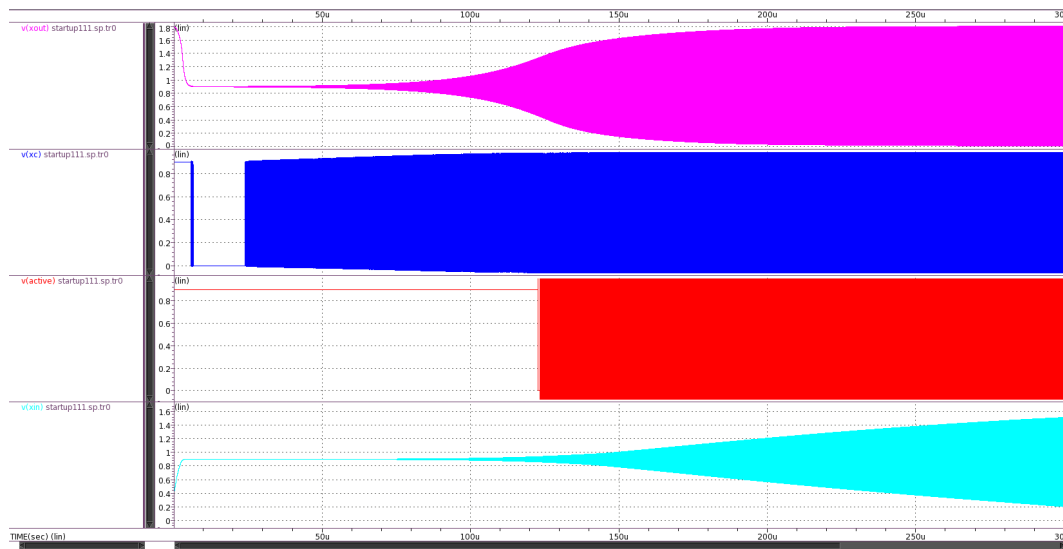


FIGURE 5.4: Transient Analysis

While performing the transient analysis, the duty cycle of the Active and XC clock has been measured and it is in the range of 46% to 52% at different PVT corners. At low power mode, when only 4 gm stages(standby mode) are connected. At PVT corners, the startup time of the crystal is varied from 120u to 154u. At PVT Current consumption at supply varies from 507uA to 890uA. The duty cycle of the Active and XC clock has been measured and it is in the range of 45% to 52% at different PVT corners.

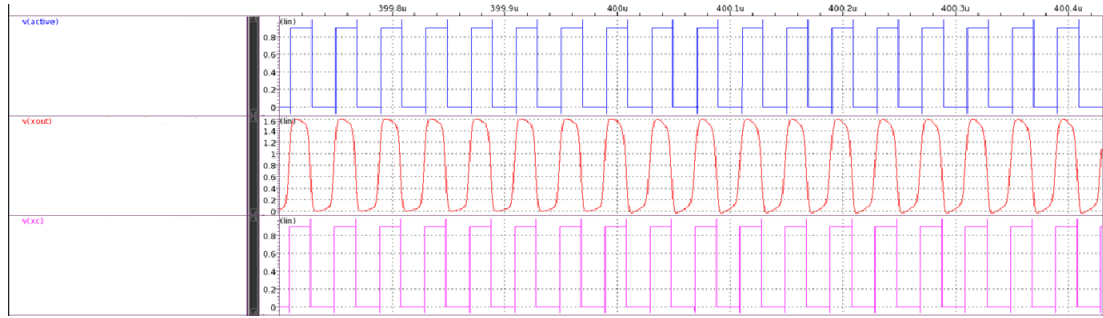


FIGURE 5.5: Close View of Transient Result

## 5.5 Phase Noise Analysis

This section contains the phase noise analysis on the proposed crystal oscillator. Fig.5.6 shows the phase noise result of the proposed crystal oscillator at XOUT, spectre simulation has been used for phase noise simulation. Due to the novel loop technique phase noise has been improved, lower the phase noise at different frequency better the noise immunity of crystal oscillator. Phase noise at 1Hz measured  $-49.711\text{dBc/Hz}$ , phase noise at 1KHz measured  $-136.67\text{dBc/Hz}$ , phase noise at 10kHz measured  $-148.21\text{dBc/Hz}$ , phase noise at 10kHz measured  $-153.97\text{dBc/Hz}$ . 2% variations have been measured in phase noise at different PVT corners.

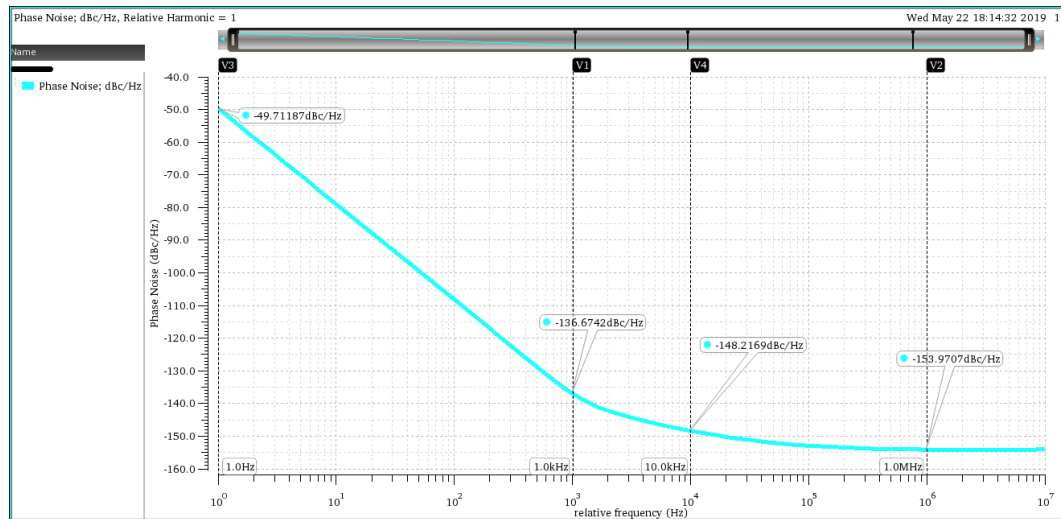


FIGURE 5.6: Phase Noise

## 5.6 Jitter Analysis

This section contains the jitter analysis on the proposed crystal oscillator. Jitter analysis has been done to check the variation due to overtone frequency(odd harmonics) on crystal frequency. Fig.5.7 shows the jitter analysis result of the proposed crystal oscillator. Jitter

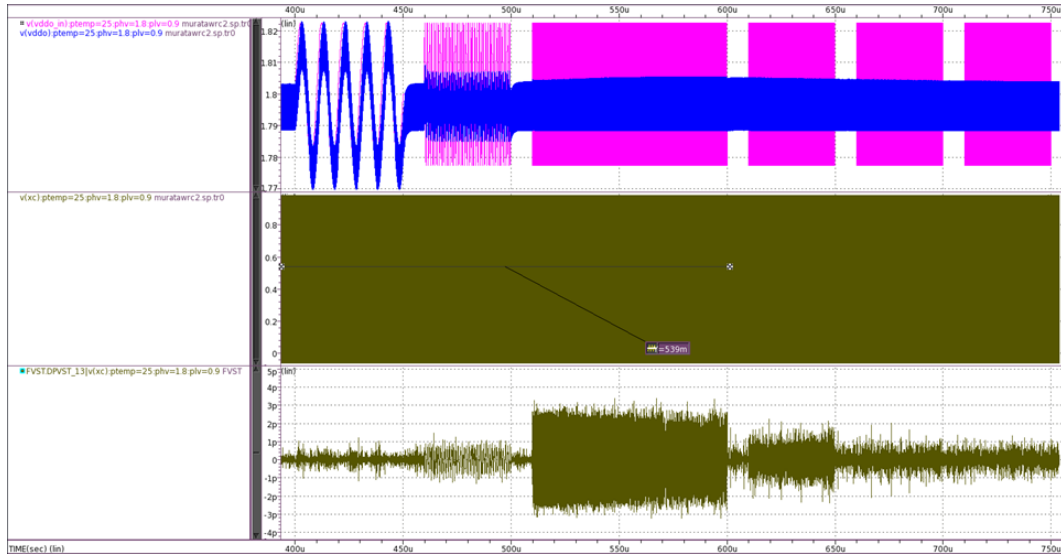


FIGURE 5.7: Jitter Analysis

is measured on the 1.8v power supply of crystal oscillator. A low pass filter has been connected at the power supply to reject the frequency greater than 1MHz. As shown in Fig.5.7 50mv of the sinusoidal pulse at different frequency starting from 100kHz, 1MHz, 12.5MHz, 37.5MHz, 62.5MHz, and 100MHz has been connected to the power supply. It has been measured that maximum jitter variation on the 12.5MHz sinusoidal power supply is 3ps. Overall jitter has measured from 1ps to 3ps at 100kHz, 1MHz, 12.5MHz, 37.5MHz, 62.5MHz, 100MHz sinusoidal frequency power supply.

## 5.7 Discussion

Table.5.1 shows the comparison of the performance metrics of the proposed crystal oscillator with the other State-of-the-Art crystal oscillator available. The present work has been noise efficient compared to the existing work. In the lowest technology node, the best phase noise has been achieved, while comparing to an existing design. This present work produced the best startup time at PVT corners compared to the existing architecture. Most of the existing work has not mentioned or calculated the jitter for odd harmonics of crystal. This work produced 3ps jitter which is the best till now. Most of the existing work used the extra circuit to reduce the power which increases the area and leads to more PVT variation. This work provides the best power consumption without increasing the overall area with less PVT variation. The duty cycle has not measured by the other state of the art. In this work, duty cycle has also been calculated. The performance has been compared with [16] [12] [1] [13] [17] [18].

TABLE 5.1: Design Comparison with existing design

Technology	28nm(This Work)	65nm[16]	65nm[12]	65nm[1]	40nm[13]	28nm[17]	90nm[18]
Supply	1.8V	1.4V	1.8V	3.3V	0.7V	1V	1.4
Oscillation Frequency	25MHz	38.4MHz	26MHz	39.25MHz	39.25MHz	48MHz	25MHz
Power( $\mu$ W)	1420	4900	1440	19	69	1500	3000
Startup Time $\mu$ S	120	1250	3200	3900	259u	-	2500
Phase Noise @1kHz	-137dBc/Hz	-135	-136	-139	-120	-114	-140
Phase Noise @1MHz	-154dBc/Hz	-	-	-153	-	-152	-152
Jitter @ $\geq$ 1MHz	3ps	-	-	-	-	-	-

## Chapter 6

# Conclusion

A novel low phase noise and fast startup time crystal oscillator has been implemented and analyzed. This thesis discusses the design, circuit implementation and the performance of the crystal oscillator to eliminate the existing design challenges. Initially, Various types of oscillators have been discussed and addressed its limitations & why crystal oscillator has been used. Due to more on-chip variations in this oscillator, the Crystal oscillator's advantages over the other oscillators are highlighted. Various parameters, property's and related work of crystal have been discussed. Noise and jitter analysis of crystal oscillator has been discussed. The advantages of the proposed transconductance stages of crystal oscillator have been discussed. This crystal oscillator is designed to generate a reference clock for PLL, which requires less phase noise & fast startup time. Drawbacks of crystal oscillators are highlighted and how the novel transconductance technique overcomes the challenges shown in the thesis.

Simulation results of the crystal oscillator transconductance stage shows (30-35)% current variations of gm stages, maximum & minimum current consumption at PVT corners found out to be 1.58mA (when all the gm stages are on) and 362uA (when only four gm stages are on) as a result at low power mode power consumption reduced. The implemented transconductance stage shows 38% open loop Gain @25MHz & 22% closed loop @25MHz variation at PVT corners. This technique leads to fast startup time which is in the range from 120u to 154u. The duty cycle variation of the clock is in between (45% - 52%). Phase noise improvement shown -136.67dBc/Hz at 1kHz and -148.21dBc/Hz at 10kHz. This technique leads to minimization in jitter which is in the range between 1ps to 3ps.

The novel crystal oscillator design is developed in TSMC 28nm CMOS technology at western digital, PVT variations have been discussed and presented thoroughly.

## 6.1 Future Work

In the current work, proposed crystal oscillator design and simulations performed at the schematic level. As future work, post layout simulations can be done to verify the design robustness against parasitic capacitance and resistances and more importantly off-chip connection of crystal oscillator. The Power consumption of the current work can be further improved by using the power management circuit.

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